LTSMIN: Distributed and Symbolic Reachability

Stefan Blom[*], Jaco van de Pol, and Michael Weber

Formal Methods and Tools, University of Twente, The Netherlands
{sccblom,vdpol,michaelw}@cs.utwente.nl

In model checking, analysis algorithms are applied to large graphs (state spaces), which model the behavior of (computer) systems. These models are typically generated from specifications in high-level languages. The LTSMIN toolset[1] provides means to generate state spaces from high-level specifications, to check safety properties on-the-fly, to store the resulting labelled transition systems (LTSs) in compressed format, and to minimize them with respect to (branching) bisimulation.

1   Motivation: A Modular, High-Performance Model Checker

The LTSMIN toolset provides a new level of modular design to high-performance model checkers. Its distinguishing feature is the wide spectrum of supported specification languages and model checking paradigms. On the language side (Sec. 3.1), it supports process algebras (MCRL), state based languages (PROMELA, DVE) and even discrete abstractions of ODE models (MAPLE, GNA). On the algorithmic side (Sec. 3.2), it supports two main streams in high-performance model checking: reachability analysis based on BDDs (symbolic) and on a cluster of workstations (distributed, enumerative). LTSMIN also incorporates a distributed implementation of state space minimization, preserving strong or branching bisimulation.

For end users, this implies that they can exploit other, scalable, verification algorithms than supported by their native tools, without changing specification language. Our experiments (Sec. 4) show that the LTSMIN toolset can match, and often outperform, existing tools tailored to their own specification language.

From an algorithm engineering point of view, LTSMIN fosters the availability of benchmark suites across multiple specification languages and verification communities. This makes benchmarking studies more robust, by separating out language-specific issues, which is of separate scientific interest. The LTSMIN toolset integrates very well with existing third-party tools (Sec. 3.3), for the benefit of their users, and also for the independent certification of model checking results.

The technical enabler of the LTSMIN toolset is its PINS interface (Sec. 2). This general abstraction of specification languages places very few constraints on their features, evident by the variety of supported languages (Sec. 3.1) and algorithms. PINS still enables the algorithms to exploit the parallel structure inherent in many specifications. Several optimizations are implemented as generic PINS2PINS wrappers, abstracting from *both*, input language and the actual model checking paradigm. Thus, this opens new opportunities for research of reusable and composable implementations of model checking algorithms and optimizations.

Language Modules

| | Process algebra: mCRL2 | State based: DVE, Promela (NIPS−VM) | ETF |

PINS

PINS2PINS Wrappers

| Local Transition Caching | Regrouping |

PINS

Reachability Tools

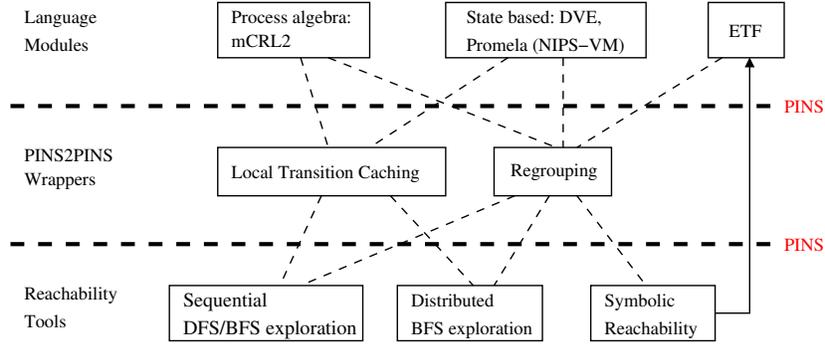| Sequential DFS/BFS exploration | Distributed BFS exploration | Symbolic Reachability |

Fig. 1. Architectural Overview of PINS-Based Tools

2 Architecture: A Partitioned Next State Interface (PINS)

In order to separate specification languages from model checking algorithms, many enumerative, on-the-fly model checkers are based on some *next-state* interface. It provides transitions between otherwise opaque and monolithic states. For example, the OPEN/CÆSAR interface [1] has been underlying the success of the CADP toolkit [2].

The unifying concept in LTSMIN is an improvement of this interface, which we call PINS, an **I**nterface based on a *Partitioned* **N**ext-**S**tate function. PINS connects language modules to analysis algorithms. The language modules compute for each specification a static dependency matrix, and implement a next-state function reflecting the operational semantics. The analysis algorithms access this abstraction of the specification, which still captures sufficient combinatorial structure to enable huge state space reductions. The key feature to this is the possibility to obtain transitions between subvectors. Due to lack of space, full details are provided elsewhere [3, 4].

In a nutshell, a state for PINS is a vector of N slots, where a single slot can represent anything. The transition relation is split disjunctively into K groups. The $K \times N$ Boolean *dependency matrix* then denotes on which slots each group might depend. Dynamically, a dependency matrix is exploited as follows. Assume that transition group k depends on a short vector of state slots $\langle x_1, \ldots, x_\ell \rangle$ only. PINS next state function operates on this short vector, yielding a short next state, say $\langle y_1, \ldots, y_\ell \rangle$. Note that this result can be reused for many concrete states. By this single call we found a set of transitions on long state vectors: $\langle x_1, \ldots, x_\ell, a_{\ell+1}, \ldots, a_N \rangle \rightarrow \langle y_1, \ldots, y_\ell, a_{\ell+1}, \ldots, a_N \rangle$.

Finally, some optimizations can be expressed purely as transformations of the PINS matrix, also rewiring next-state calls. Such building blocks are implemented once, but all combinations of specification languages and analysis tools can benefit (Fig. 1).

The LTSMIN toolset consists of 28,000 lines of C Code.[2] The interfacing code for the supported frontends (DVE, NIPS, μCRL, mCRL2, our own ETF, Sec. 3.3) consists of only 200–500 lines each. The majority of code is in the three reachability tools, their support data structures, PINS2PINS wrappers, and the TORX [5] and CADP [1] connectors. Taken together, this yields 25 tool combinations, in addition to the minimization tool and various other support tools. The toolset is tested on Linux and MacOS X.

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[2] measured with David A. Wheeler's 'SLOCCount'.

3 Functionality

3.1 Multiple Specification Languages

State-Based Languages. We implemented a language module for the DVE implementation of Barnat el al., giving access to the BEEM benchmark database [6]. Another language module connects the NIPSVM state generator [7], an interpreter for PROMELA, giving access to (pure) SPIN models [8]. The latter module could be refined by making the dependency matrix sparser for global variables and channels, which in general would improve the performance of the reachability tools.

Process Algebras. We have connected the native state generators of the μCRL [9] and mCRL2 [10] toolsets to LTSMIN. Both toolsets specify models in ACP-style process algebra with data, and are heavily used in industrial case studies [9]. They provide expressive ways to model systems, e.g., abstract data types (unbounded numbers, lists, trees), constrained data enumeration, and multi-way handshake communication.

Through the link with LTSMIN, users of all these tools gain for free 100% compatible enumerative, symbolic and distributed model checking tools, as well as compact state space storage formats and minimization tools.

3.2 Reachability and Minimization Tools

We implemented several tools for high-performance state space generation, in particular based on symbolic and distributed model checking. All exploration tools can check safety properties on-the-fly, and produce counter examples upon property violation. Alternatively, full state spaces can be generated and stored for minimization and analysis by external third-party model checkers.

Sequential: Implementations of standard enumerative reachability algorithms, using BFS or DFS search order. These PINS-based tools allow a base-line comparison with the native space generation facilities.

Symbolic: Implementations of symbolic reachability tools. Sets of states are stored as *(binary) decision diagrams*. The state space is computed symbolically by applications of the relational product. More precisely, for any specification language with an enumerative state generator implementing PINS, we automatically obtain a symbolic generator [3, 4].

Distributed: Implementations of distributed state space generators, now based on the PINS interface, generalizing our earlier work [11]. This effectively combines the memory of many workstations, also achieving considerable speedups.

PINS2PINS *wrappers:* All generators profit from optimizations in the PINS2PINS layer (Fig. 1). *Local transition caching* is useful for both enumerative generators; *tree compression* [11] is a technique for reducing memory footprint of enumerative generators; and *variable reordering* and *transition regrouping* [3] are useful for the symbolic generator, and in combination with transition caching.

Finally, in case of full state space generation, the LTSMIN toolset includes the distributed minimization tool `ltsmin-mpi` for (strong and branching) bisimulation reduction of labelled transition systems [12]. Also, Orzan's distributed τ-cycle elimination `ce-mpi` [13] tool is included. τ-Cycle freeness in turn admits the use of a simplified distributed minimization algorithm [14] for branching bisimulation. State based equivalences could be easily obtained by modifying the initial partition.

3.3 Tool Interoperability

Besides connecting to native state space generators of various languages (Sec. 3.1), LTSMIN provides converters or interfaces to third party back-end model checkers.

ETF. We defined our own Extended Table Format,[3] which enumerates all short transitions for all groups. It serves as input language of PINS, and as concise output format. E.g., we saw a 0.57 billion state LTS fit in a 1.6 Kb ETF file.

CADP and μCRL. LTSMIN has connections to the well-known CADP toolbox. State spaces can be exported in *binary coded graph* (BCG) format. LTSMIN also implements the CÆSAR/OPEN interface [1] to CADP's on-the-fly model checking and bisimulation algorithms. State spaces can be converted in μCRL's DIR format, allowing to use and compare against *their* implementation of distributed minimization tools.

DIVINE framework. The LTSMIN toolset includes a converter (`etf2dve`) from our ETF format to the input language of the DIVINE toolset [15], DVE. Thus, we obtain access to DIVINE's battery of distributed model checking algorithms. An interesting application is the certification of model checking results, to improve user confidence.

TORX testing tool. LTSMIN implements the TORX RPC interface (⟨*spec*⟩2torx), which allows *test case derivation* with TORX [5] for all PINS language modules. Additionally, JTORX allows checking two specifications for ioco-conformance [16].

GNA tool. In EC-MOAN,[4] the Genetic Network Analyzer [17] exports discrete abstractions of biological ODE models to ETF, and LTSMIN generates their state space for further analysis.

4 Experiments

We performed extensive benchmarking. Precise experimental results go beyond the scope of this tool paper. As illustration, the log-log scatter plot in Fig. 2 shows how distributed and symbolic model checking tools complement each other on selected DVE models from the *BEnchmarks for **Explicit** Model Checkers* (BEEM) database [6], ranging from 3×10^6 to 0.57×10^9 states. Each point represents two runs for one specification. The vertical axis indicates the wall-clock

Fig. 2. Wall-clock time in seconds for distributed (x) and symbolic (y) reachability

time (in seconds) for symbolic reachability (using variable reordering and the chaining heuristic); the horizontal axis denotes the time taken by distributed reachability (on 8×6 cores; with transition caching). The two models near the bottom-right corner are cases where symbolic methods are more than two orders of magnitude faster, whereas for `lift.[78]` and `pgm_protocol.8` the distributed tool is faster by more than factor 10. These are the first reported BDD-based experiments on benchmarks from the BEEM database, whose models are naturally biased towards enumerative methods.
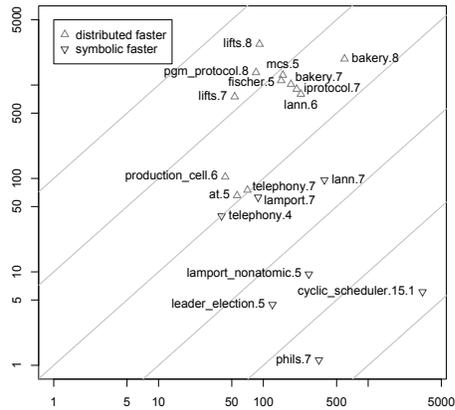
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[3] http://fmt.cs.utwente.nl/tools/ltsmin/etf.html

[4] European FP6 project on biological cell modeling and analysis, see http://www.ec-moan.org/

In INESS,[5] LTSmin is used for the safety analysis of novel railway interlocking specifi-
cations. XUML statecharts are translated to MCRL2, and analyzed for safety properties
by LTSMIN [18]. Depending on the track layout, we generated state spaces of up to
1.5×10^{11} states directly from MCRL2 models, by means of our symbolic tools.

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[5] European FP7 project on INtegrated European Signalling Systems, http://www.iness.eu/

Appendix: For Review Only

A Availability

At the time of writing, the sixth public release of LTSmin, version 1.5, is available under an open-source (BSD-style) licence at ⟨http://fmt.cs.utwente.nl/tools/ltsmin/⟩. The initial version of the toolset was released in November 2008. This tool paper is the first to summarize its features.

B Benchmarks

Table 1. Benchmark results from Fig. 2 in tabular form. We measured wall-clock times in seconds on a cluster of Quad-core Dual Intel Xeon 5335 processors and 8 Gigabyte memory per node. Each test had exclusive access to the machines. The distributed tests were all performed using 6 cores per machine on 8 machines, without fine-tuning when less machines would have sufficed.

BEEM Model	Reachability Times [sec]		States	Transitions
	Distributed	Symbolic		
at.5	56.19	65.52	31,999,440	125,231,180
bakery.7	183.44	1,017.24	29,047,471	100,691,444
bakery.8	595.30	1,901.82	253,131,202	1,074,134,374
cyclic_scheduler.15.1	3,300.40	6.11	574,021,814	3,252,910,440
fischer.5	147.94	1,117.16	101,028,339	477,823,470
iprotocol.7	207.96	901.69	59,794,192	200,828,479
lamport_nonatomic.5	89.08	9.46	38,717,846	160,667,630
lamport.7	271.73	63.02	95,118,524	505,734,961
lann.6	228.27	798.24	144,151,628	648,779,852
lann.7	382.73	96.41	160,025,986	944,322,648
leader_election.5	122.04	4.47	4,803,952	28,064,092
lifts.7	53.27	748.58	5,126,781	13,631,916
lifts.8	91.96	2,736.56	12,359,648	31,993,172
mcs.5	153.58	1,275.25	60,556,519	278,302,279
pgm_protocol.8	85.11	1,361.32	3,069,390	7,125,121
phils.7	339.17	1.14	71,934,773	893,796,878
production_cell.6	43.28	103.90	14,520,700	45,593,810
telephony.4	39.88	39.73	12,291,552	64,110,312
telephony.7	70.57	75.09	21,960,308	114,070,470

Short Name	Command Line
Distributed	`dve2lts-mpi --cache --regroups=gs` *model*
Symbolic	`dve-reach --order=chain --regroup=gs --vset=list` *model*

C Output of Sample Run

```
Command line: dve-reach --order=chain -rgs --vset=list cyclic_scheduler.15.1.dve cyc_sched.etf
dve-reach: Exploration order is chain
dve-reach: opening cyclic_scheduler.15.1.dve
Reading DVE source...
Compiling DVE source... done
dve-reach: Regroup specification: gs
[...]
dve-reach: Regrouping: 60->45 groups
dve-reach: Creating an AtermDD list domain.
dve-reach: length is 60, there are 45 groups
dve-reach: got initial state
dve-reach: visited 0 has 1 states ( 62 nodes )
dve-reach: visited 1 has 28 states ( 156 nodes )
dve-reach: visited 2 has 49150 states ( 298 nodes )
dve-reach: visited 3 has 81918 states ( 310 nodes )
dve-reach: visited 4 has 196606 states ( 328 nodes )
dve-reach: visited 5 has 360446 states ( 345 nodes )
dve-reach: visited 6 has 606206 states ( 364 nodes )
dve-reach: visited 7 has 974846 states ( 381 nodes )
dve-reach: visited 8 has 1527806 states ( 397 nodes )
dve-reach: visited 9 has 2357246 states ( 414 nodes )
dve-reach: visited 10 has 3601406 states ( 432 nodes )
dve-reach: visited 11 has 5467646 states ( 450 nodes )
dve-reach: visited 12 has 8267006 states ( 466 nodes )
dve-reach: visited 13 has 12466046 states ( 483 nodes )
dve-reach: visited 14 has 18764606 states ( 500 nodes )
dve-reach: visited 15 has 28212446 states ( 517 nodes )
[...]
dve-reach: visited 31 has 526546418 states ( 828 nodes )
dve-reach: visited 32 has 550638410 states ( 827 nodes )
dve-reach: visited 33 has 564455876 states ( 647 nodes )
dve-reach: visited 34 has 569238845 states ( 644 nodes )
dve-reach: visited 35 has 574021814 states ( 645 nodes )
dve-reach: Exploration took 1620 group checks and 1620 next state calls
dve-reach: reachability took 0.980 real 0.970 user 0.020 sys
state space has 574021814 states
( 645 final BDD nodes; 828 peak nodes )
[...]
dve-reach: writing output took 0.020 real 0.010 user 0.000 sys
Exit [0]
5.93 user, 0.19 system, 6.20 elapsed -- Max VSize = 73196KB, Max RSS = 19756KB
```

Size[bytes]	File	Description
11,140	`cyclic_scheduler.15.1.dve`	Input specification (DVE format)
831	`cyclic_scheduler.15.1.dve.bz2`	Compressed with `bzip2`
55,438	`cyc_sched.15.1.etf`	Fully generated state space in ETF format
1,574	`cyc_sched.15.1.etf.bz2`	Compressed with `bzip2`